

Practicing Dissipative Particle Dynamics

Yu-Hang Tang

CSRC, September 24, 2015



Pacific Northwest
NATIONAL LABORATORY

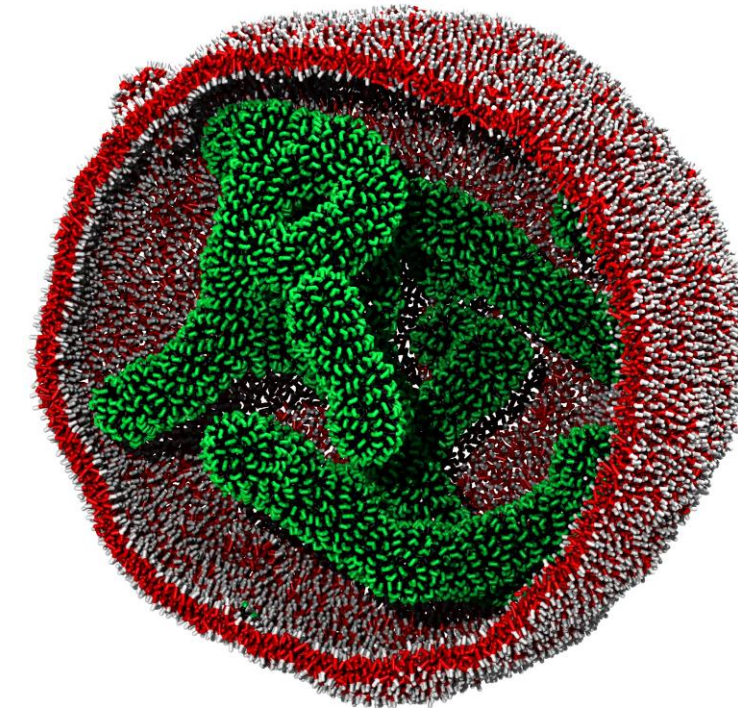
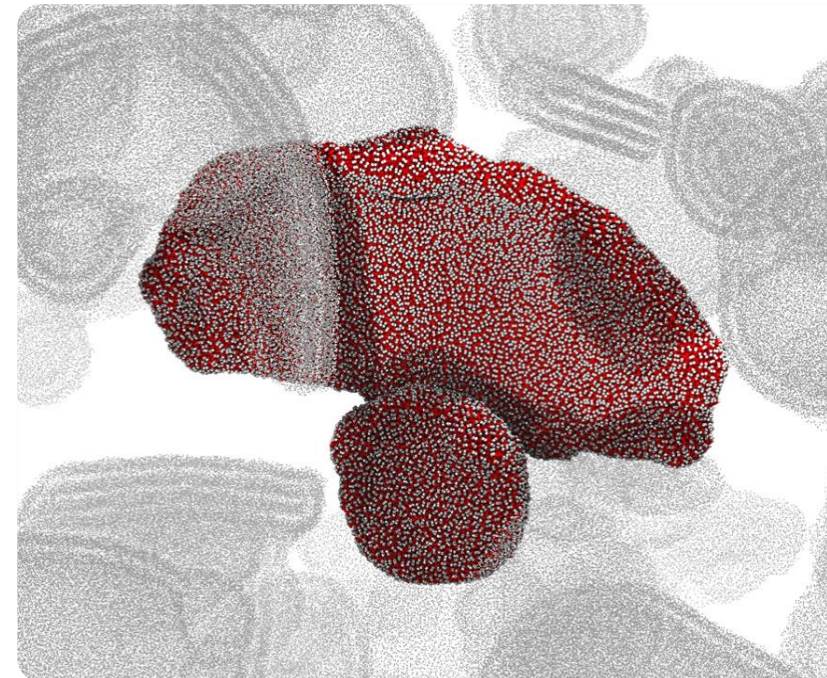
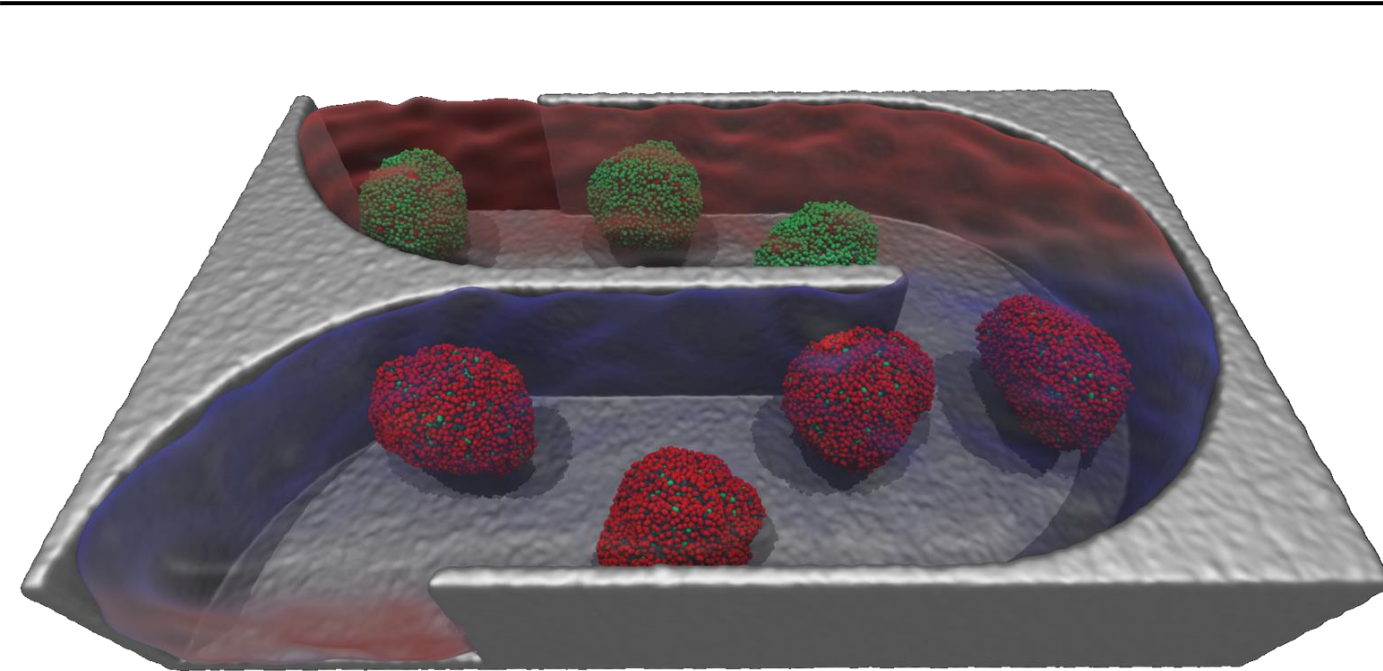
Proudly Operated by **Battelle** Since 1965

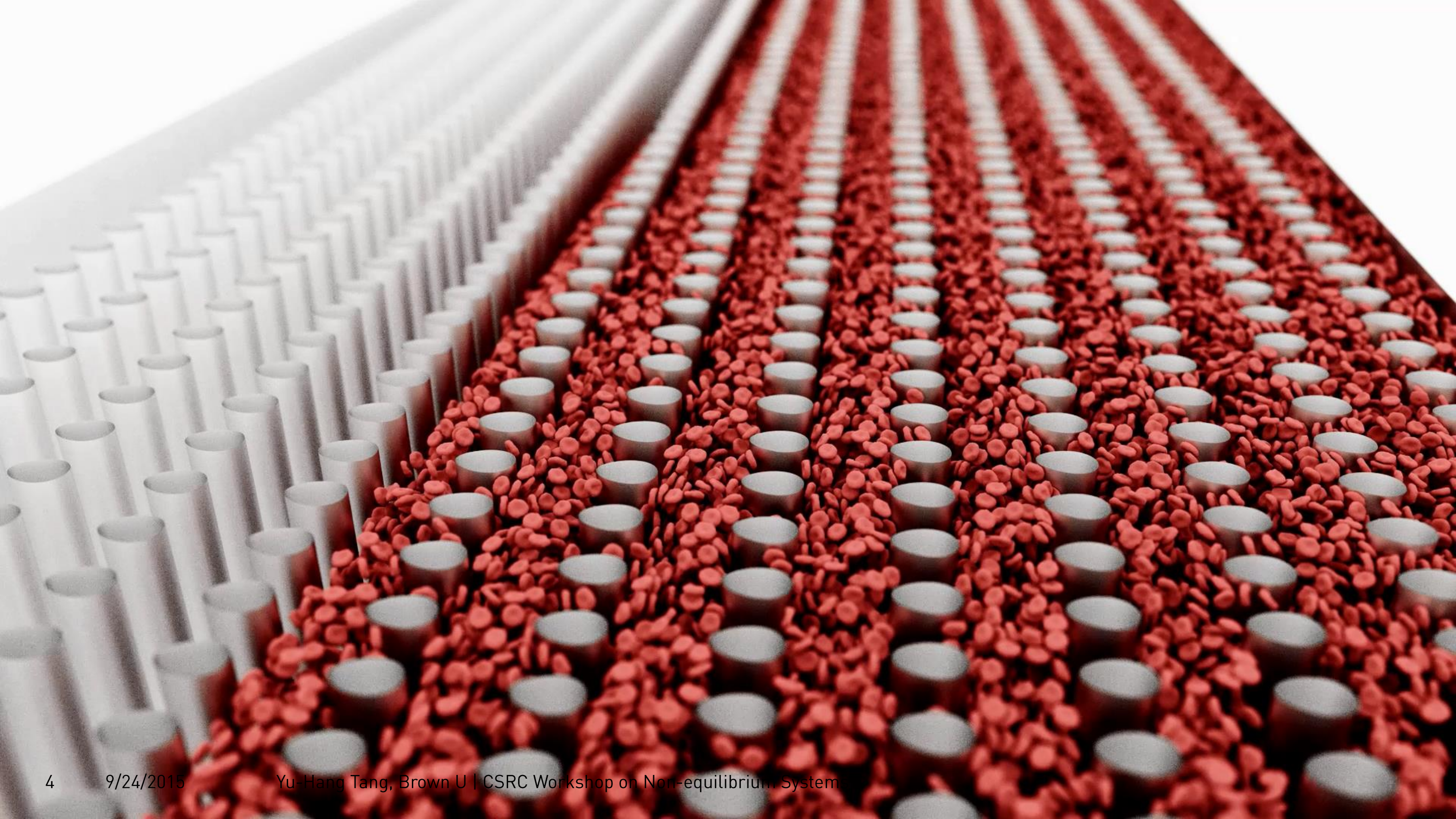
CM4
Collaboratory on Mathematics for
Mesoscopic Modeling of Materials

Format: Discussion-based

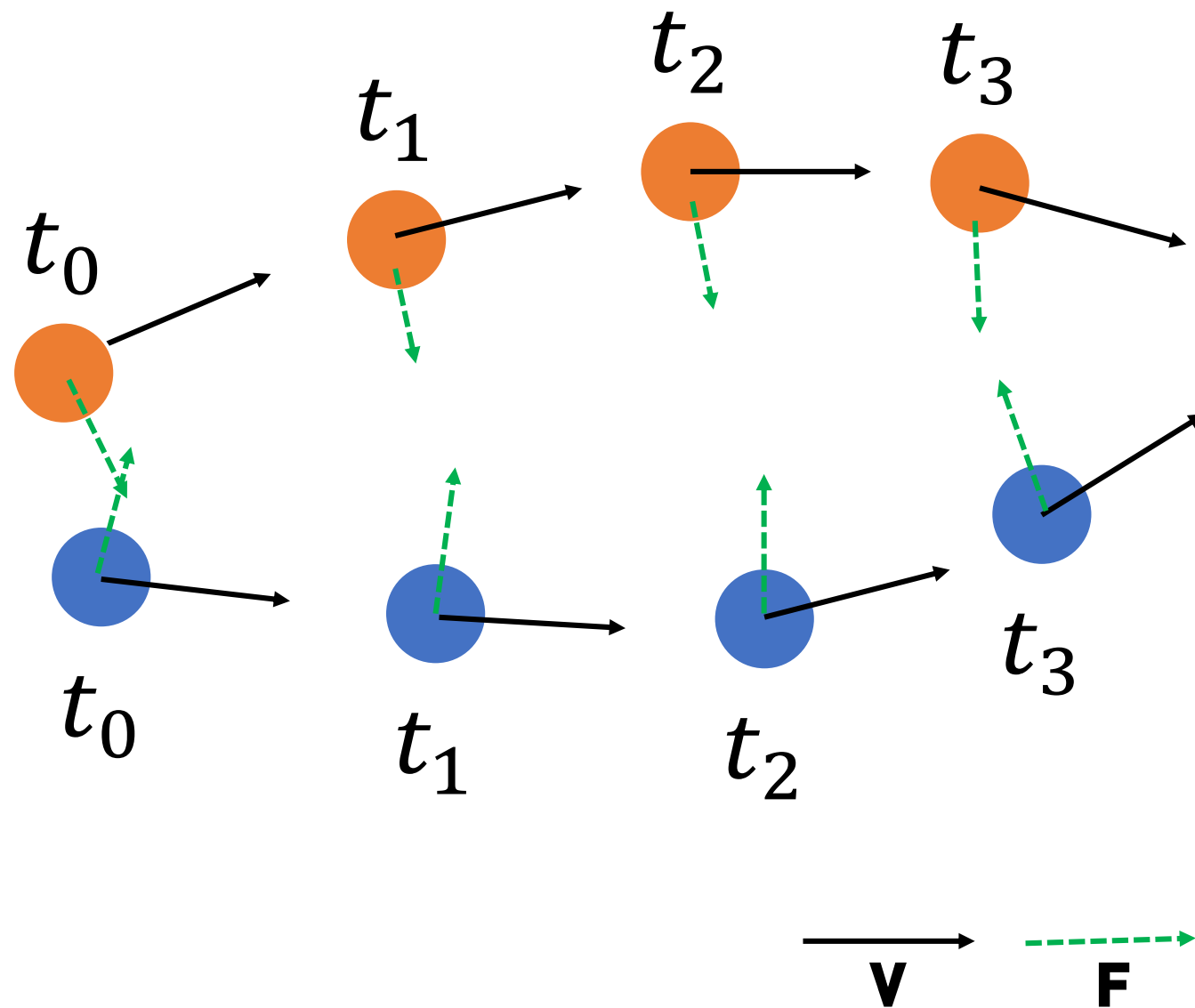
Feel free to interrupt at any time!

Dissipative Particle Dynamics is a **stochastic, particle-based** technique for simulating simple and complex fluids.





In DPD we track the **motion of particles**.



$$m \cdot a(t) = f = -\frac{\partial H}{\partial x(t)}$$

$$v\left(t + \frac{\Delta t}{2}\right) = v(t) + \frac{1}{2}a(t)\Delta t$$

$$x(t + \Delta t) = x(t) + v\left(t + \frac{\Delta t}{2}\right)\Delta t$$

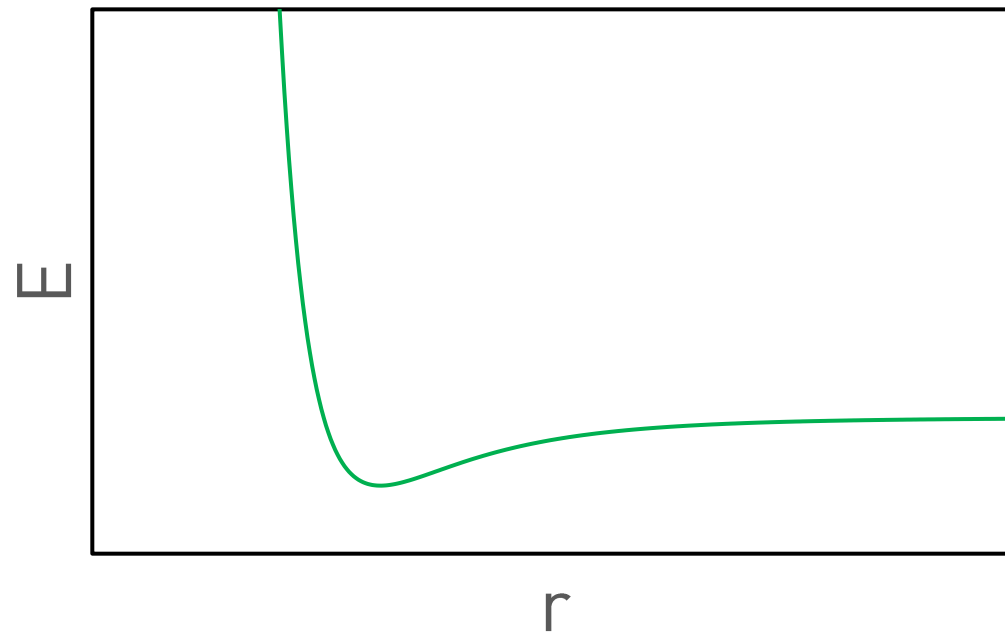
$$a(t + \Delta t) = -\frac{\partial H}{\partial x(t + \Delta t)}$$

$$v(t + \Delta t) = v\left(t + \frac{\Delta t}{2}\right) + \frac{1}{2}a(t + \Delta t)\Delta t$$

Short-range **pairwise** interactions

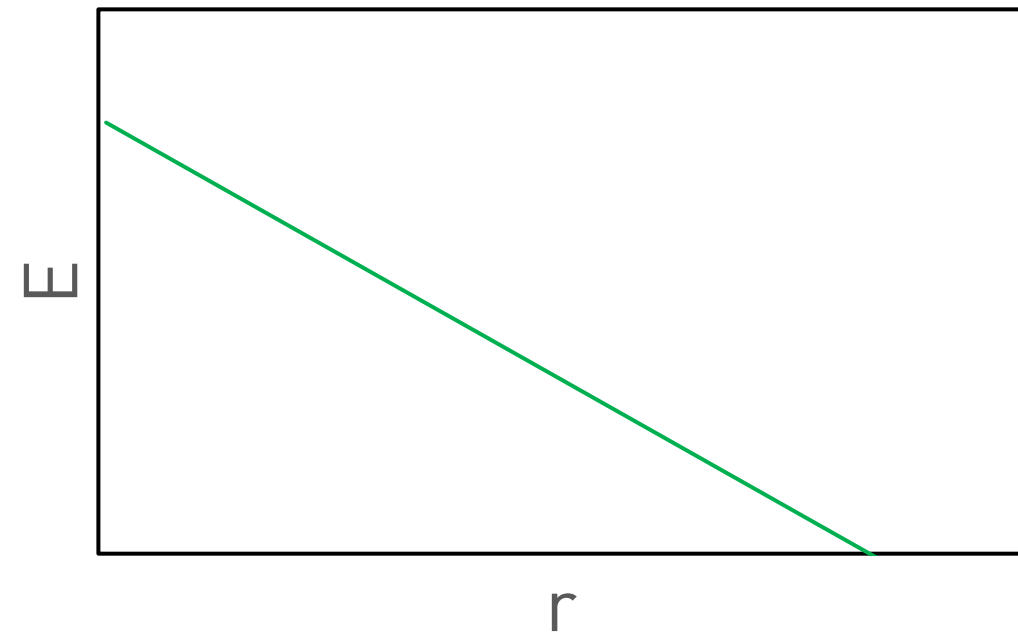
Lenard-Jones Potential

$$\sigma \left[-2 \left(\frac{r}{r_0} \right)^6 + \left(\frac{r}{r_0} \right)^{12} \right]$$



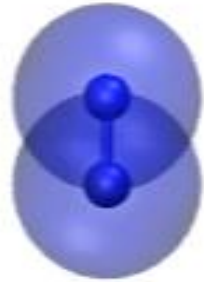
DPD Linear Force

$$a_{ij} \left[1 - \frac{r}{r_0} \right]$$

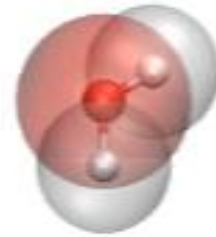


Bonded potential

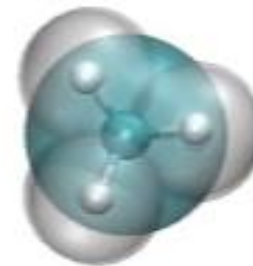
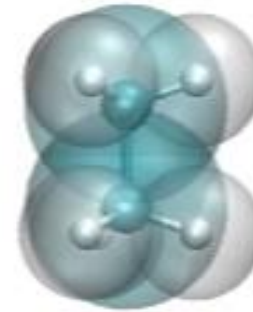
Bond



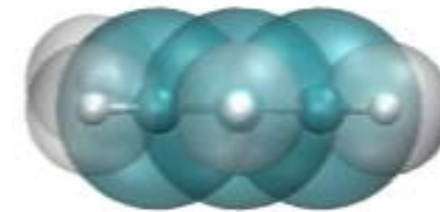
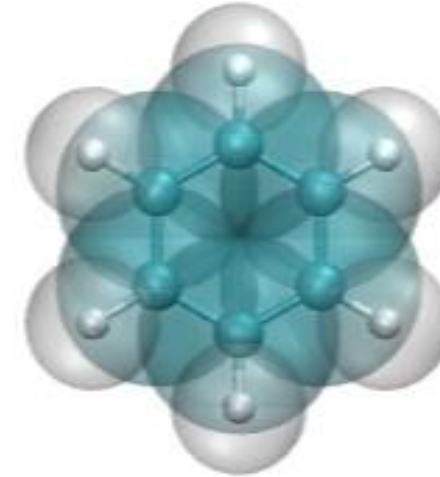
Angle



Dihedral



Improper

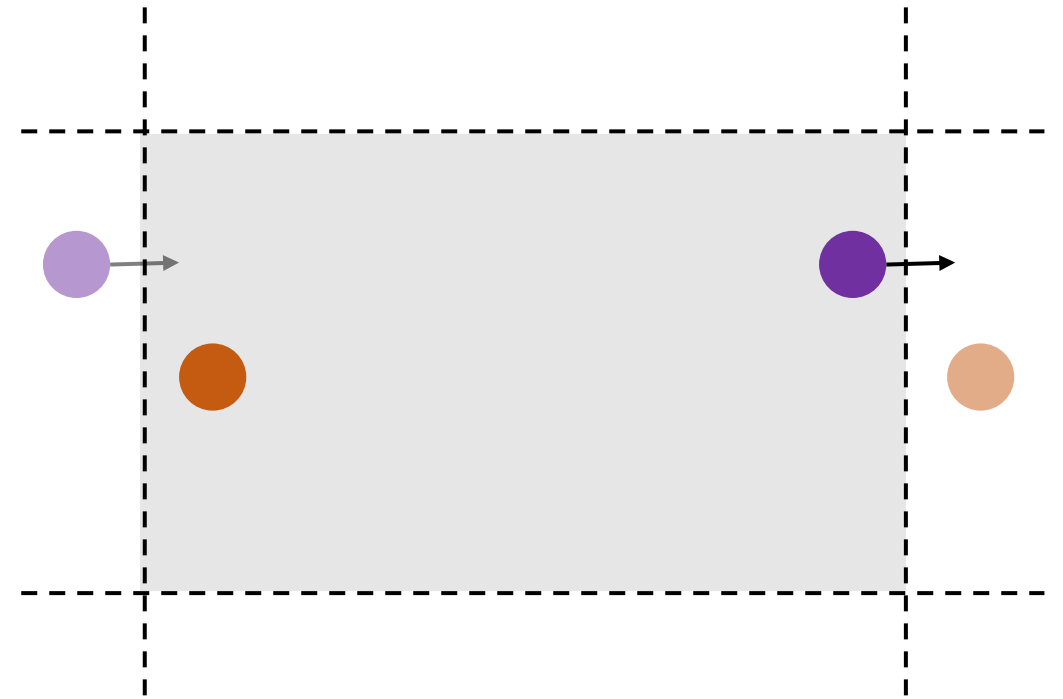


Periodic boundary conditions

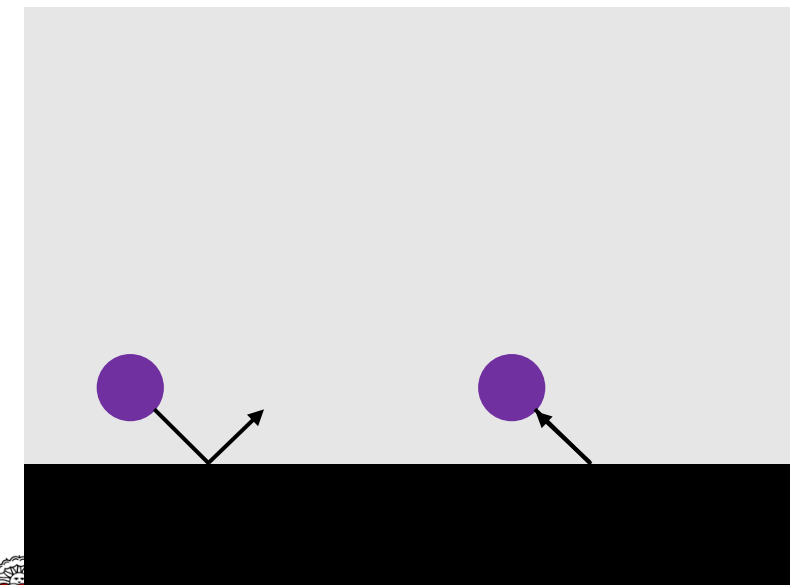
approximate infinite systems by tiling unit cells.

A particle passing through the boundary re-appears on the opposite side with the same velocity.

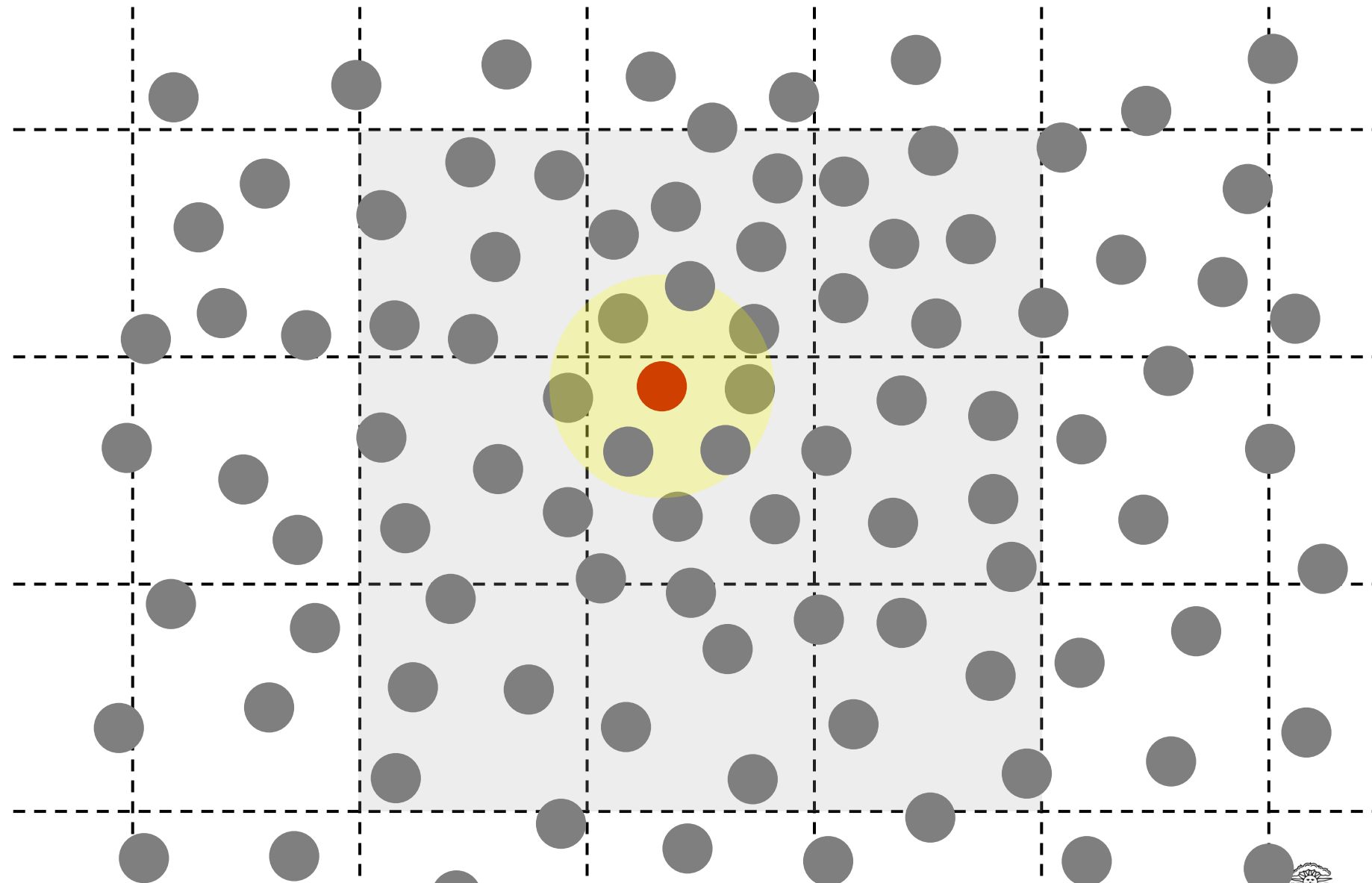
minimum image convention



Bounce forward/back conditions

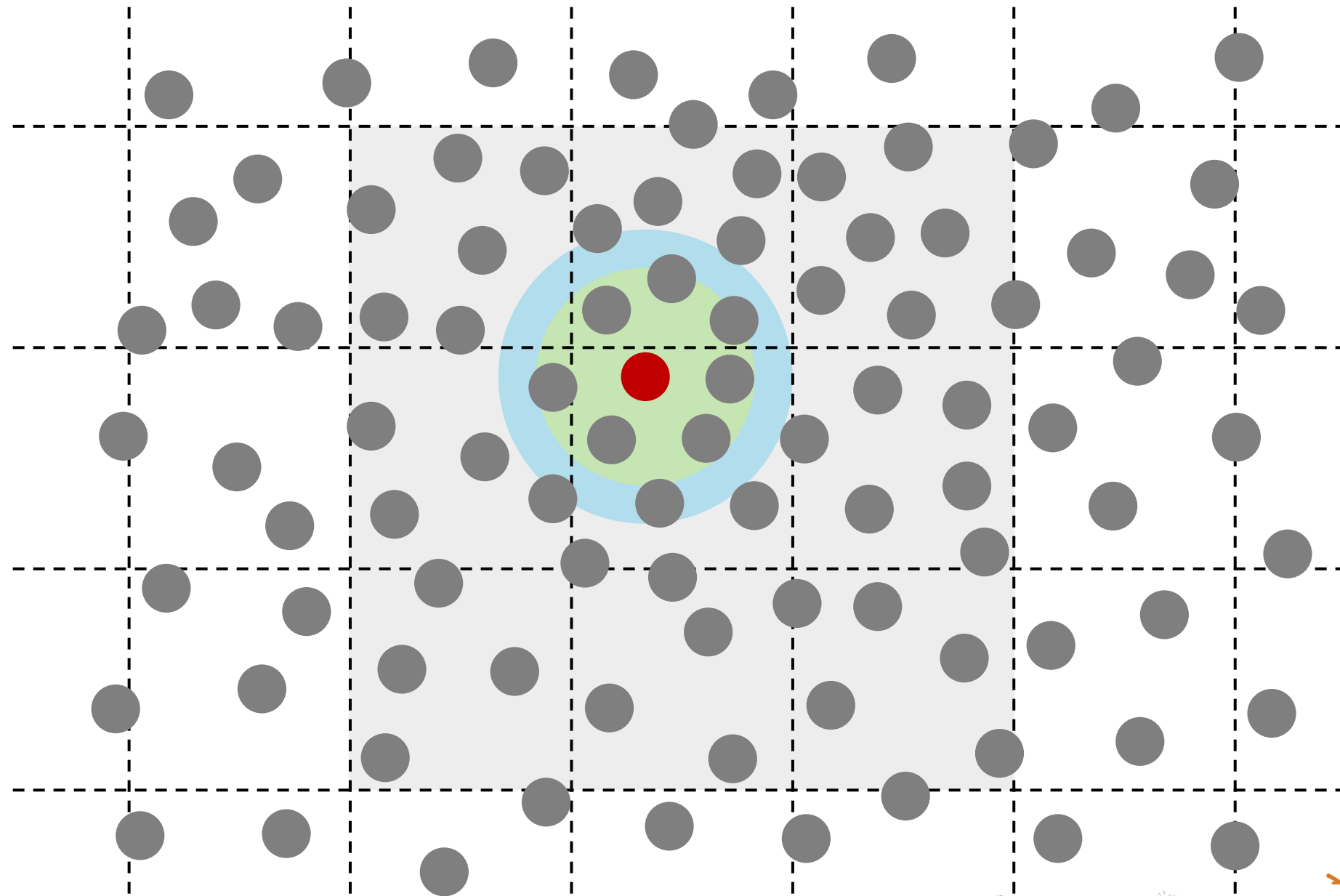


The **cell list** algorithm is ubiquitously employed to accelerate the evaluation of pairwise forces.

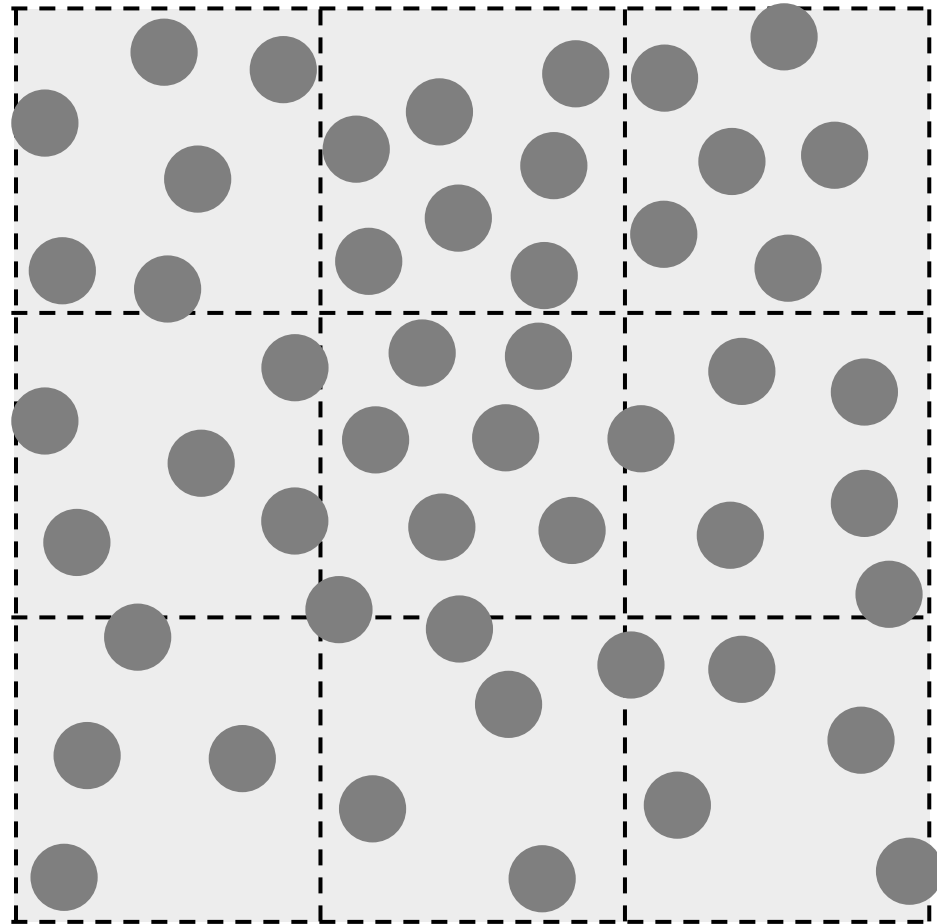


$O(N^2)$ to $O(N)$

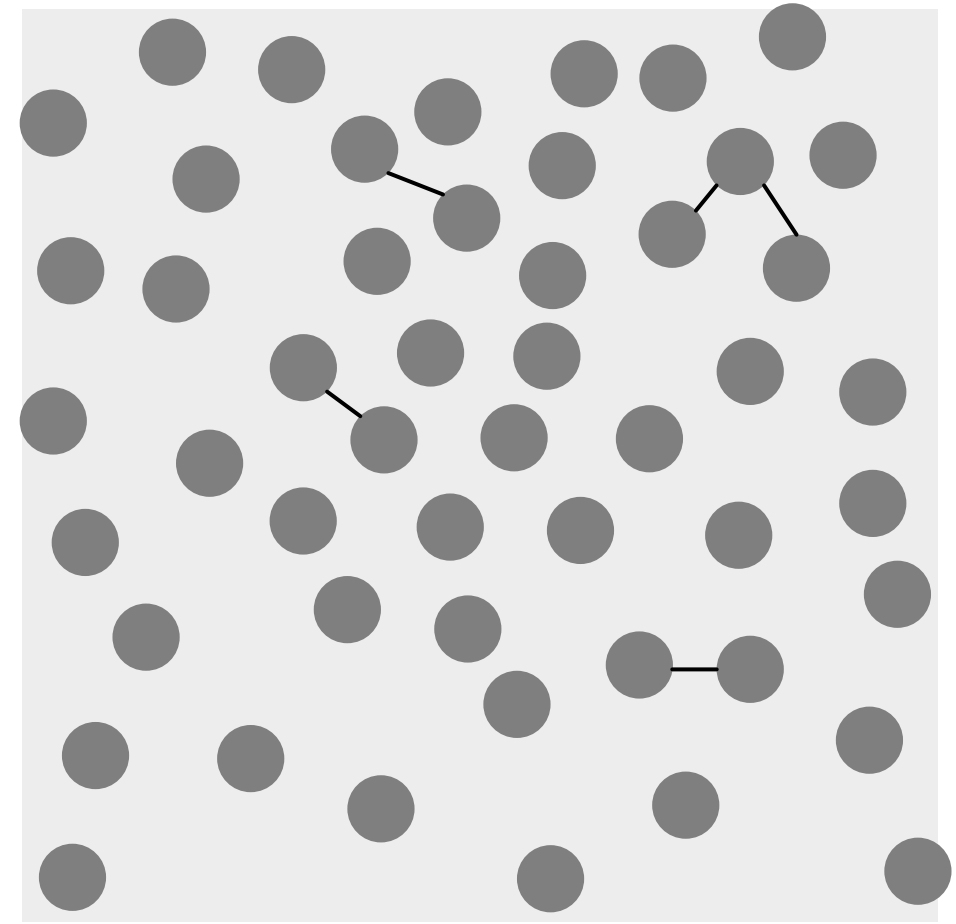
A **neighbor list** with skin distance may be even faster.



Domain decomposition



Task decomposition



LAMMPS

=

Large-scale **A**tomic/**M**olecular **M**assively **P**arallel **S**imulator

<http://lammps.sandia.gov/>

- ✓ model particles at the atomic, meso, or continuum scale.
- ✓ serial or parallel using message-passing spatial decomposition
- ✓ easy to modify or extend
- ✓ open source (GPL)

Installation

Step 1. Download source

```
svn co svn://svn.lammps.org/lammps-ro/trunk lammps
```

Step 2. Compile

```
cd lammps/src
```

```
make serial OR make mpi
```

Step 3. Verify compilation

```
cd lammps/bench
```

```
../src/lmp_serial -in in.lj
```

```
mpirun -np 2 ../src/lmp_mpi -in in.lj
```

Enable **optional packages**

Molecule package

```
make yes-molecule
```

USER MESO package (requires CUDA and MPI)

```
svn co http://www.cfm.brown.edu/repo/release/USER-MESO/ meso
```

```
cd meso
```

```
make yes-molecule
```

```
make yes-user-meso
```

```
make meso
```

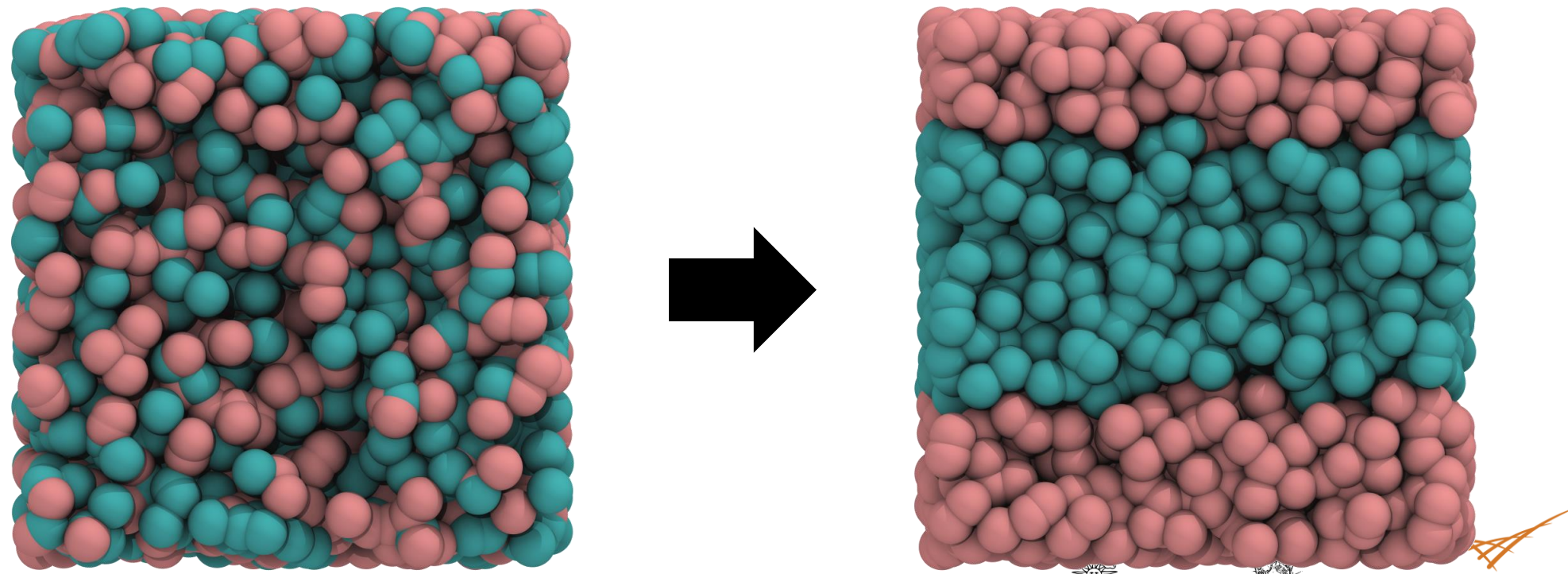

Example I: Binary Immiscible liquid

Script at

<http://www.cfm.brown.edu/repo/release/DPD-workshop/binary.lmp>

Once finished, visualize with VMD

```
vmd binary.lammpstrj
```



Line-by-line: # DPD binary mixture

```
# DPD binary mixture
dimension      3
units          lj
comm_modify    vel yes
newton         off

atom_style     atomic
neighbor       0.3 bin
neigh_modify   delay 0 every 4 check no

region         domain block -5 5 -5 5 -5 5 units box
create_box     2 domain
lattice        fcc 4
create_atoms   1 random 1500 15255 domain
create_atoms   2 random 1500 47214 domain
mass           * 1.0

pair_style     dpd 1.0 1.0 419084618
pair_coeff     1 1 25.0 4.5
pair_coeff     1 2 150.0 4.5
pair_coeff     2 2 25.0 4.5

thermo         100
dump          dump0 all atom 5 binary.lammpstrj

velocity       all create 1.0 8178251
fix            integrator all nve

timestep       0.01
run            10000
```

A comment. Specifically, the # sign may appear anywhere in a line, and all characters from there onward are treated as comment and discarded.

Line-by-line: dimension 3

```
# DPD binary mixture
dimension 3
units lj
comm_modify vel yes
newton off

atom_style atomic
neighbor 0.3 bin
neigh_modify delay 0 every 4 check no

region domain block -5 5 -5 5 -5 5 units box
create_box 2 domain
lattice fcc 4
create_atoms 1 random 1500 15255 domain
create_atoms 2 random 1500 47214 domain
mass * 1.0

pair_style dpd 1.0 1.0 419084618
pair_coeff 1 1 25.0 4.5
pair_coeff 1 2 150.0 4.5
pair_coeff 2 2 25.0 4.5

thermo 100
dump dump0 all atom 5 binary.lampstrj

velocity all create 1.0 8178251
fix integrator all nve

timestep 0.01
run 10000
```

Set the dimensionality of the simulation

syntax: dimension N

N: 2 or 3

Line-by-line: units lj

```
# DPD binary mixture
dimension      3
units          lj
comm_modify    vel yes
newton         off

atom_style     atomic
neighbor       0.3 bin
neigh_modify   delay 0 every 4 check no

region         domain block -5 5 -5 5 -5 5 units box
create_box     2 domain
lattice        fcc 4
create_atoms   1 random 1500 15255 domain
create_atoms   2 random 1500 47214 domain
mass           * 1.0

pair_style     dpd 1.0 1.0 419084618
pair_coeff     1 1 25.0 4.5
pair_coeff     1 2 150.0 4.5
pair_coeff     2 2 25.0 4.5

thermo         100
dump          dump0 all atom 5 binary.lammpstrj

velocity      all create 1.0 8178251
fix           integrator all nve

timestep      0.01
run           10000
```

Set the unit used in the simulation to be 'lj', i.e. reduced units.

Line-by-line: comm_modify vel yes

```
# DPD binary mixture
dimension      3
units          lj
comm_modify    vel yes
newton         off

atom_style     atomic
neighbor       0.3 bin
neigh_modify   delay 0 every 4 check no

region         domain block -5 5 -5 5 -5 5 units box
create_box     2 domain
lattice        fcc 4
create_atoms   1 random 1500 15255 domain
create_atoms   2 random 1500 47214 domain
mass           * 1.0

pair_style     dpd 1.0 1.0 419084618
pair_coeff     1 1 25.0 4.5
pair_coeff     1 2 150.0 4.5
pair_coeff     2 2 25.0 4.5

thermo         100
dump           dump0 all atom 5 binary.lammpstrj

velocity       all create 1.0 8178251
fix            integrator all nve

timestep       0.01
run            10000
```

Exchange velocity data of particles during MPI parallel execution; necessary for DPD.

Line-by-line: newton off

```
# DPD binary mixture
dimension      3
units          lj
comm_modify    vel yes
newton         off

atom_style     atomic
neighbor       0.3 bin
neigh_modify   delay 0 every 4 check no

region         domain block -5 5 -5 5 -5 5 units box
create_box     2 domain
lattice        fcc 4
create_atoms   1 random 1500 15255 domain
create_atoms   2 random 1500 47214 domain
mass           * 1.0

pair_style     dpd 1.0 1.0 419084618
pair_coeff     1 1 25.0 4.5
pair_coeff     1 2 150.0 4.5
pair_coeff     2 2 25.0 4.5

thermo         100
dump          dump0 all atom 5 binary.lammpstrj

velocity      all create 1.0 8178251
fix           integrator all nve

timestep      0.01
run           10000
```

Whether or not to exploit Newton's 3rd law to accelerate computation.

Syntax: newton on|off

Setting newton to on accelerates serial computation but may lower performance at high parallelism; newton off mandatory for GPU acceleration.

Line-by-line: atom_style atomic

```
# DPD binary mixture
dimension      3
units          lj
comm_modify    vel yes
newton         off

atom_style      atomic
neighbor        0.3 bin
neigh_modify    delay 0 every 4 check no

region          domain block -5 5 -5 5 -5 5 units box
create_box      2 domain
lattice         fcc 4
create_atoms    1 random 1500 15255 domain
create_atoms    2 random 1500 47214 domain
mass            * 1.0

pair_style      dpd 1.0 1.0 419084618
pair_coeff       1 1 25.0 4.5
pair_coeff       1 2 150.0 4.5
pair_coeff       2 2 25.0 4.5

thermo          100
dump            dump0 all atom 5 binary.lampstrj

velocity        all create 1.0 8178251
fix             integrator all nve

timestep        0.01
run             10000
```

Select style of atom container.

Syntax: atom_style style

style = atomic, bond, full, etc.

Each atom style carries a different set of degrees of freedom.

Line-by-line: neighbor 0.3 bin

```
# DPD binary mixture
dimension      3
units          lj
comm_modify    vel yes
newton         off

atom_style     atomic
neighbor       0.3 bin
neigh_modify   delay 0 every 4 check no

region         domain block -5 5 -5 5 -5 5 units box
create_box     2 domain
lattice        fcc 4
create_atoms   1 random 1500 15255 domain
create_atoms   2 random 1500 47214 domain
mass           * 1.0

pair_style     dpd 1.0 1.0 419084618
pair_coeff     1 1 25.0 4.5
pair_coeff     1 2 150.0 4.5
pair_coeff     2 2 25.0 4.5

thermo         100
dump           dump0 all atom 5 binary.lampstrj

velocity       all create 1.0 8178251
fix            integrator all nve

timestep       0.01
run            10000
```

Select style of neighbor list.

Syntax: neighbor skin style

skin = skin distance

style = bin | nsq

Line-by-line: neigh_modify delay 0 every 4 check no

```
# DPD binary mixture
dimension      3
units          lj
comm_modify    vel yes
newton         off

atom_style     atomic
neighbor       0.3 bin
neigh_modify   delay 0 every 4 check no

region         domain block -5 5 -5 5 -5 5 units box
create_box     2 domain
lattice        fcc 4
create_atoms   1 random 1500 15255 domain
create_atoms   2 random 1500 47214 domain
mass           * 1.0

pair_style     dpd 1.0 1.0 419084618
pair_coeff     1 1 25.0 4.5
pair_coeff     1 2 150.0 4.5
pair_coeff     2 2 25.0 4.5

thermo         100
dump           dump0 all atom 5 binary.lammpstrj

velocity       all create 1.0 8178251
fix            integrator all nve

timestep       0.01
run            10000
```

Configure neighbor list update frequency.

Syntax: every M delay N check yes|no

delay: wait for N steps before rebuilding

every: rebuild neighbor list every M steps

check: only rebuild if some atom has moved more than half the skin.

Line-by-line: region domain block -5 5 -5 5 -5 5 units box

```
# DPD binary mixture
dimension      3
units          lj
comm_modify    vel yes
newton         off

atom_style     atomic
neighbor       0.3 bin
neigh_modify   delay 0 every 4 check no

region         domain block -5 5 -5 5 -5 5 units box
create_box     2 domain
lattice        fcc 4
create_atoms   1 random 1500 15255 domain
create_atoms   2 random 1500 47214 domain
mass           * 1.0

pair_style     dpd 1.0 1.0 419084618
pair_coeff     1 1 25.0 4.5
pair_coeff     1 2 150.0 4.5
pair_coeff     2 2 25.0 4.5

thermo         100
dump           dump0 all atom 5 binary.lampstrj

velocity       all create 1.0 8178251
fix            integrator all nve

timestep       0.01
run            10000
```

Define a region in the 3D space for later use; multiple regions can be define within each simulation

Syntax: region ID style args

In this case we built a cubic region of size 10x10x10 centered at the origin

Line-by-line: create_box 2 domain

```
# DPD binary mixture
dimension      3
units          lj
comm_modify   vel yes
newton         off

atom_style     atomic
neighbor       0.3 bin
neigh_modify   delay 0 every 4 check no

region         domain block -5 5 -5 5 -5 5 units box
create_box    2 domain
lattice        fcc 4
create_atoms   1 random 1500 15255 domain
create_atoms   2 random 1500 47214 domain
mass           * 1.0

pair_style     dpd 1.0 1.0 419084618
pair_coeff     1 1 25.0 4.5
pair_coeff     1 2 150.0 4.5
pair_coeff     2 2 25.0 4.5

thermo         100
dump           dump0 all atom 5 binary.lampstrj

velocity       all create 1.0 8178251
fix            integrator all nve

timestep       0.01
run            10000
```

Create a simulation box based on the region previously defined.

Syntax: create_box N region

N: max number of atom types used in the simulation

Line-by-line: lattice fcc 4

```
# DPD binary mixture
dimension      3
units          lj
comm_modify   vel yes
newton         off

atom_style     atomic
neighbor       0.3 bin
neigh_modify   delay 0 every 4 check no

region         domain block -5 5 -5 5 -5 5 units box
create_box     2 domain
lattice      fcc 4
create_atoms   1 random 1500 15255 domain
create_atoms   2 random 1500 47214 domain
mass           * 1.0

pair_style     dpd 1.0 1.0 419084618
pair_coeff     1 1 25.0 4.5
pair_coeff     1 2 150.0 4.5
pair_coeff     2 2 25.0 4.5

thermo         100
dump           dump0 all atom 5 binary.lampstrj

velocity       all create 1.0 8178251
fix            integrator all nve

timestep       0.01
run            10000
```

Define a lattice for the subsequent 'create_atoms' command

Syntax: lattice style scale

style = none | sc | bcc | fcc etc...

Note: this line is actually unused in the presented script but will be part of an exercise.

Line-by-line: `create_atoms 1 random 1500 15255 domain`

```
# DPD binary mixture
dimension      3
units          lj
comm_modify    vel yes
newton         off

atom_style     atomic
neighbor       0.3 bin
neigh_modify   delay 0 every 4 check no

region         domain block -5 5 -5 5 -5 5 units box
create_box     2 domain
lattice        fcc 4
create_atoms  1 random 1500 15255 domain
create_atoms  2 random 1500 47214 domain
mass          * 1.0

pair_style     dpd 1.0 1.0 419084618
pair_coeff     1 1 25.0 4.5
pair_coeff     1 2 150.0 4.5
pair_coeff     2 2 25.0 4.5

thermo        100
dump          dump0 all atom 5 binary.lammpstrj

velocity      all create 1.0 8178251
fix           integrator all nve

timestep      0.01
run           10000
```

Create atoms randomly in the simulation box

Syntax: `create_atoms type style args`

Specifically: `create_atoms type random N seed region`

type: type of the created particles

N: number of particles to create

seed: seed for random number generator

region: only create atoms in the region

Line-by-line: mass * 1.0

```
# DPD binary mixture
dimension      3
units          lj
comm_modify   vel yes
newton         off

atom_style     atomic
neighbor       0.3 bin
neigh_modify   delay 0 every 4 check no

region         domain block -5 5 -5 5 -5 5 units box
create_box     2 domain
lattice        fcc 4
create_atoms   1 random 1500 15255 domain
create_atoms   2 random 1500 47214 domain
mass          * 1.0

pair_style     dpd 1.0 1.0 419084618
pair_coeff     1 1 25.0 4.5
pair_coeff     1 2 150.0 4.5
pair_coeff     2 2 25.0 4.5

thermo         100
dump           dump0 all atom 5 binary.lammpstrj

velocity       all create 1.0 8178251
fix            integrator all nve

timestep       0.01
run            10000
```

Set the mass for each type of particle

Syntax: mass type value

type: number or range or *

m: type m

n*: all types from n to N

*n: all types from 1 to n

m*n: all types from m to n

*: all types

Line-by-line: `pair_style dpd 1.0 1.0 419084618`

```
# DPD binary mixture
dimension      3
units          lj
comm_modify    vel yes
newton         off

atom_style     atomic
neighbor       0.3 bin
neigh_modify   delay 0 every 4 check no

region         domain block -5 5 -5 5 -5 5 units box
create_box     2 domain
lattice        fcc 4
create_atoms   1 random 1500 15255 domain
create_atoms   2 random 1500 47214 domain
mass           * 1.0

pair_style     dpd 1.0 1.0 419084618
pair_coeff     1 1 25.0 4.5
pair_coeff     1 2 150.0 4.5
pair_coeff     2 2 25.0 4.5

thermo         100
dump           dump0 all atom 5 binary.lampstrj

velocity       all create 1.0 8178251
fix            integrator all nve

timestep       0.01
run            10000
```

Use the DPD style for pairwise force evaluation.

Syntax: `pair_style dpd $k_B T$ r_c seed`

$k_B T$: temperature

r_c : cutoff distance

seed: seed for random number generator

Line-by-line: pair_coeff 1 1 25.0 4.5

```
# DPD binary mixture
dimension      3
units          lj
comm_modify    vel yes
newton         off

atom_style     atomic
neighbor       0.3 bin
neigh_modify   delay 0 every 4 check no

region         domain block -5 5 -5 5 -5 5 units box
create_box     2 domain
lattice        fcc 4
create_atoms   1 random 1500 15255 domain
create_atoms   2 random 1500 47214 domain
mass           * 1.0

pair_style     dpd 1.0 1.0 419084618
pair_coeff     1 1 25.0 4.5
pair_coeff     1 2 150.0 4.5
pair_coeff     2 2 25.0 4.5

thermo         100
dump           dump0 all atom 5 binary.lampstrj

velocity       all create 1.0 8178251
fix            integrator all nve

timestep       0.01
run            10000
```

Set up pairwise coefficients

Syntax: pair_coeff type1 type2 A gamma [r_c]

A: conservative force constant

gamma: dissipation strength

r_c (optional): cutoff for a specific pair

Line-by-line: thermo 100

```
# DPD binary mixture
dimension      3
units          lj
comm_modify    vel yes
newton         off

atom_style     atomic
neighbor       0.3 bin
neigh_modify   delay 0 every 4 check no

region         domain block -5 5 -5 5 -5 5 units box
create_box     2 domain
lattice        fcc 4
create_atoms   1 random 1500 15255 domain
create_atoms   2 random 1500 47214 domain
mass           * 1.0

pair_style     dpd 1.0 1.0 419084618
pair_coeff     1 1 25.0 4.5
pair_coeff     1 2 150.0 4.5
pair_coeff     2 2 25.0 4.5

thermo       100
dump          dump0 all atom 5 binary.lampstrj

velocity      all create 1.0 8178251
fix           integrator all nve

timestep      0.01
run           10000
```

display diagnostics every N steps

Line-by-line: `dump dump0 all atom 5 binary.lammpstrj`

```
# DPD binary mixture
dimension      3
units          lj
comm_modify    vel yes
newton         off

atom_style     atomic
neighbor       0.3 bin
neigh_modify   delay 0 every 4 check no

region         domain block -5 5 -5 5 -5 5 units box
create_box     2 domain
lattice        fcc 4
create_atoms   1 random 1500 15255 domain
create_atoms   2 random 1500 47214 domain
mass          * 1.0

pair_style     dpd 1.0 1.0 419084618
pair_coeff     1 1 25.0 4.5
pair_coeff     1 2 150.0 4.5
pair_coeff     2 2 25.0 4.5

thermo        100
dump          dump0 all atom 5 binary.lammpstrj

velocity      all create 1.0 8178251
fix           integrator all nve

timestep      0.01
run           10000
```

Configure trajectory output

Syntax: `dump ID group style args`

ID: ID for the dump; multiple dumps with different IDs may be defined within a simulation.

group: the groups of particles to dump; a group 'all' containing all particles is predefined in LAMMPS

style: atom – LAMMPS's own trajectory format; may also be dcd, xyz etc.

`args|atom = N filename`

Line-by-line: **velocity all create 1.0 8178251**

```
# DPD binary mixture
dimension      3
units          lj
comm_modify   vel yes
newton         off

atom_style     atomic
neighbor       0.3 bin
neigh_modify   delay 0 every 4 check no

region         domain block -5 5 -5 5 -5 5 units box
create_box     2 domain
lattice        fcc 4
create_atoms   1 random 1500 15255 domain
create_atoms   2 random 1500 47214 domain
mass           * 1.0

pair_style     dpd 1.0 1.0 419084618
pair_coeff     1 1 25.0 4.5
pair_coeff     1 2 150.0 4.5
pair_coeff     2 2 25.0 4.5

thermo         100
dump           dump0 all atom 5 binary.lampstrj

velocity      all create 1.0 8178251
fix            integrator all nve

timestep       0.01
run            10000
```

Set particle initial velocity

Syntax: velocity group style args

Specifically:

velocity group create T seed

velocity group set vx vy vz

Line-by-line: fix integrator all nve

```
# DPD binary mixture
dimension      3
units          lj
comm_modify    vel yes
newton         off

atom_style     atomic
neighbor       0.3 bin
neigh_modify   delay 0 every 4 check no

region         domain block -5 5 -5 5 -5 5 units box
create_box     2 domain
lattice        fcc 4
create_atoms   1 random 1500 15255 domain
create_atoms   2 random 1500 47214 domain
mass           * 1.0

pair_style     dpd 1.0 1.0 419084618
pair_coeff     1 1 25.0 4.5
pair_coeff     1 2 150.0 4.5
pair_coeff     2 2 25.0 4.5

thermo         100
dump          dump0 all atom 5 binary.lampstrj

velocity      all create 1.0 8178251
fix          integrator all nve

timestep      0.01
run           10000
```

Uses the NVE integrator as a 'LAMMPS fix'.

Syntax: fix ID group style

Line-by-line: timestep 0.01

```
# DPD binary mixture
dimension      3
units          lj
comm_modify    vel yes
newton         off

atom_style     atomic
neighbor       0.3 bin
neigh_modify   delay 0 every 4 check no

region         domain block -5 5 -5 5 -5 5 units box
create_box     2 domain
lattice        fcc 4
create_atoms   1 random 1500 15255 domain
create_atoms   2 random 1500 47214 domain
mass           * 1.0

pair_style     dpd 1.0 1.0 419084618
pair_coeff     1 1 25.0 4.5
pair_coeff     1 2 150.0 4.5
pair_coeff     2 2 25.0 4.5

thermo         100
dump          dump0 all atom 5 binary.lampstrj

velocity       all create 1.0 8178251
fix           integrator all nve

timestep       0.01
run           10000
```

Set time step size

Line-by-line: run 10000

```
# DPD binary mixture
dimension      3
units          lj
comm_modify   vel yes
newton         off

atom_style     atomic
neighbor       0.3 bin
neigh_modify   delay 0 every 4 check no

region         domain block -5 5 -5 5 -5 5 units box
create_box     2 domain
lattice        fcc 4
create_atoms   1 random 1500 15255 domain
create_atoms   2 random 1500 47214 domain
mass           * 1.0

pair_style     dpd 1.0 1.0 419084618
pair_coeff     1 1 25.0 4.5
pair_coeff     1 2 150.0 4.5
pair_coeff     2 2 25.0 4.5

thermo         100
dump           dump0 all atom 5 binary.lampstrj

velocity       all create 1.0 8178251
fix            integrator all nve

timestep       0.01
run            10000
```

Run the simulation for 10000 steps

Instead of 'creating' particles we can also load them through **data file**.

Each atom style takes a slightly different format, i.e. different # of columns in the Atoms section, etc.

Check LAMMPS website for the specifics

```
# data file sample
```

```
1000 atoms
```

```
1 atom types
```

```
0 10 xlo xhi
```

```
0 10 ylo yhi
```

```
0 10 zlo zhi
```

```
Masses
```

```
1 1.000000
```

```
Atoms
```

```
1 1 8.401877172 3.943829268 7.830992238
```

```
2 1 7.984400335 9.116473579 1.975513693
```

```
3 1 3.352227557 7.682295948 2.777747108
```

```
...
```

Style

Styles is the mechanism used by LAMMPS to allow scalable functionality extension.

From a user's perspective they serve as options to various LAMMPS commands.

From a developer's perspective they are C++ derived classes of a virtual base class. Overloading the virtual interfaces allows the custom functionalities to be implemented.

Groups

A group is a collection of particles. The group ID can be used in other commands such as fix, compute, dump, or velocity to act on those atoms together.

Syntax:

```
group ID style args
```

```
style = region, type, etc...
```


Fix

A 'fix' is any operation that is applied to the system during time stepping. Examples include updating of atom positions and velocities due to time integration, controlling temperature, applying constraint forces to atoms, enforcing boundary conditions, computing diagnostics, etc.

Fixes perform their operations at different stages of the timestep.

Advanced topic: implementing custom fixes

Verlet scheme, stages and fix class

Thank you for attending!

Y.H.T. appreciates invitation and support from **Dr. Zhen Li, Dr. Zhewei Zhou, Dr. George Karaniadakis,** and **Shanghai Institute of Applied Mathematics and Mechanics, Shanghai Center for Nonlinear Sciences, Pacific Northwest National Lab,** and **Beijing Computational Science Research Center.**



Pacific Northwest
NATIONAL LABORATORY

Proudly Operated by **Battelle** Since 1965

CM4
Collaboratory on Mathematics for
Mesoscopic Modeling of Materials